

A train is moving on a straight track with speed  $20 \text{ ms}^{-1}$ . It is blowing its whistle at the frequency of  $1000 \text{ Hz}$ . The percentage change in the frequency heard by a person standing near the track as the train passes him is (speed of sound =  $320 \text{ ms}^{-1}$ ) close to :

- (1) 12%
- (2) 18%
- (3) 24%
- (4) 6%

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We have,  $f_{heard} = f \left( \frac{V + V_{listener}}{V - V_{source}} \right)$  with appropriate signs for  $V_{listener}$  and  $V_{source}$ .

$f' = 1000 \times \left( \frac{320}{320 - 20} \right) = \frac{32,000}{30}$  when the train is approaching

$f'' = 1000 \times \left( \frac{320}{320 + 20} \right) = \frac{32,000}{34}$  when the train is moving away

$$\begin{aligned} \text{\% change in frequency} &= \frac{f' - f''}{f'} \times 100 \\ &= \frac{\frac{32,000}{30} - \frac{32,000}{34}}{\frac{32,000}{30}} \times 100 = \frac{\frac{1}{30} - \frac{1}{34}}{\frac{1}{30}} \times 100 \\ &= \frac{4}{34} \times 100 \approx 12\% \end{aligned}$$

Hence, Option (1).