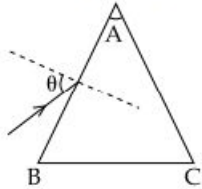


Monochromatic light is incident on a glass prism of angle A . If the refractive index of the material of the prism is μ , a ray, incident at an angle θ , on the face AB would get transmitted through the face AC of the prism provided :



$$(1) \quad \theta < \sin^{-1} \left[\mu \sin \left(A - \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$$

$$(2) \quad \theta > \cos^{-1} \left[\mu \sin \left(A + \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$$

$$(3) \quad \theta < \cos^{-1} \left[\mu \sin \left(A + \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$$

$$(4) \quad \theta > \sin^{-1} \left[\mu \sin \left(A - \sin^{-1} \left(\frac{1}{\mu} \right) \right) \right]$$

For AB , we have

$$\sin \theta = \mu \sin r \quad \dots\dots\dots(*)$$

For AC , the condition for total internal reflection is $\mu \sin C = 1$

Since, we do not want total internal reflection $r' < C$

$$\therefore \sin r' < \sin C$$

$$\therefore \mu \sin r' < \mu \sin C$$

$$\therefore \mu \sin r' < 1 \quad \dots\dots\dots(#)$$

Now, $r + r' = A$

$$\therefore r' = A - r$$

$$\therefore \sin r' = \sin(A - r) < \frac{1}{\mu} \quad \text{[From (#)]}$$

$$\therefore A - r < \sin^{-1} \frac{1}{\mu}$$

$$\therefore r > A - \sin^{-1} \frac{1}{\mu}$$

$$\therefore \sin r > \sin \left(A - \sin^{-1} \frac{1}{\mu} \right)$$

$$\therefore \frac{\sin \theta}{\mu} > \sin \left(A - \sin^{-1} \frac{1}{\mu} \right) \quad \text{[From (*)]}$$

$$\therefore \sin \theta > \mu \sin \left(A - \sin^{-1} \frac{1}{\mu} \right)$$

$$\therefore \theta > \sin^{-1} \left(\mu \sin \left(A - \sin^{-1} \frac{1}{\mu} \right) \right)$$

Hence, option (4).