

An ideal gas undergoes a quasi static, reversible process in which its molar heat capacity  $C$  remains constant. If during this process the relation of pressure  $P$  and volume  $V$  is given by  $PV^n = \text{constant}$ , then  $n$  is given by (Here  $C_p$  and  $C_v$  are molar specific heat at constant pressure and constant volume, respectively) :

$$(1) \quad n = \frac{C_p}{C_v}$$

$$(2) \quad n = \frac{C - C_p}{C - C_v}$$

$$(3) \quad n = \frac{C_p - C}{C - C_v}$$

$$(4) \quad n = \frac{C - C_v}{C - C_p}$$

( $n$  denotes number of moles)

Based on JEE Main 2016

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$$dQ = dU + dW$$

$$\therefore nCdT = nC_vdT + PdV$$

$$\therefore n(C - C_v)dT = PdV \dots\dots\dots(1)$$

Now,  $PV^n = \text{constant}$

$$\therefore PV = nRT, TV^{n-1} = \text{constant}$$

Or,  $\ln T + (n-1)\ln V = \text{constant}$

$$\therefore \frac{dT}{T} + (n-1)\frac{dV}{V} = 0$$

$$\text{Or, } VdT = (1-n)TdV \dots\dots\dots(2)$$

$$\text{From (1) \& (2), } \frac{n(C - C_v)}{V} = \frac{P}{(1-n)T}$$

$$\therefore n(C - C_v) = \frac{1}{(1-n)} \frac{PV}{T} = \frac{1}{(1-n)} nR$$

$$\therefore (C - C_v) = \frac{R}{(1-n)} = \frac{C_p - C_v}{1-n}$$

$$\therefore 1-n = \frac{C_p - C_v}{C - C_v}$$

$$\therefore n = 1 - \frac{C_p - C_v}{C - C_v} = \frac{C - C_p}{C - C_v}$$

Hence, Option (2).